



Oxford Cambridge and RSA

AS Level Further Mathematics B (MEI)

Y410/01 Core Pure

Question Paper

Monday 14 May 2018 – Afternoon

Time allowed: 1 hour 15 minutes



You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

You may use:

- a scientific or graphical calculator

INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the barcodes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION

- The total number of marks for this paper is **60**.
- The marks for each question are shown in brackets [].
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

Answer **all** the questions.

- 1 The matrices **A**, **B** and **C** are defined as follows:

$$\mathbf{A} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 2 & 0 & 3 \\ 1 & -1 & 3 \end{pmatrix}, \quad \mathbf{C} = (1 \ 3).$$

Calculate all possible products formed from two of these three matrices. [4]

- 2 Find, to the nearest degree, the angle between the vectors $\begin{pmatrix} 1 \\ 0 \\ -2 \end{pmatrix}$ and $\begin{pmatrix} -2 \\ 3 \\ -3 \end{pmatrix}$. [3]

- 3 Find real numbers a and b such that $(a - 3i)(5 - i) = b - 17i$. [5]

- 4 Find a cubic equation with real coefficients, two of whose roots are $2 - i$ and 3 . [5]

- 5 A transformation of the x - y plane is represented by the matrix $\begin{pmatrix} \cos \theta & 2 \sin \theta \\ 2 \sin \theta & -\cos \theta \end{pmatrix}$, where θ is a positive acute angle.

(i) Write down the image of the point $(2, 3)$ under this transformation. [2]

(ii) You are given that this image is the point $(a, 0)$. Find the value of a . [5]

- 6 Find the invariant line of the transformation of the x - y plane represented by the matrix $\begin{pmatrix} 2 & 0 \\ 4 & -1 \end{pmatrix}$. [4]

- 7 (i) Express $\frac{1}{2r-1} - \frac{1}{2r+1}$ as a single fraction. [2]

(ii) Find how many terms of the series

$$\frac{2}{1 \times 3} + \frac{2}{3 \times 5} + \frac{2}{5 \times 7} + \dots + \frac{2}{(2r-1)(2r+1)} + \dots$$

are needed for the sum to exceed 0.999 999. [7]

- 8 Prove by induction that $\begin{pmatrix} 1 & 1 \\ 0 & 2 \end{pmatrix}^n = \begin{pmatrix} 1 & 2^n - 1 \\ 0 & 2^n \end{pmatrix}$ for all positive integers n . [6]

- 9 Fig. 9 shows a sketch of the region OPQ of the Argand diagram defined by

$$\{z : |z| \leq 4\sqrt{2}\} \cap \left\{z : \frac{1}{4}\pi \leq \arg z \leq \frac{1}{3}\pi\right\}.$$

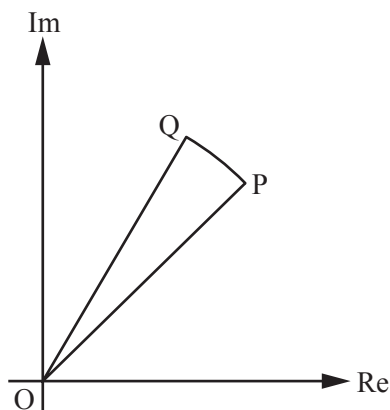


Fig. 9

- (i) Find, in modulus-argument form, the complex number represented by the point P. [2]
- (ii) Find, in the form $a + ib$, where a and b are exact real numbers, the complex number represented by the point Q. [3]
- (iii) **In this question you must show detailed reasoning.**

Determine whether the points representing the complex numbers

- $3 + 5i$
- $5.5(\cos 0.8 + i \sin 0.8)$

lie within this region.

[4]

- 10 Three planes have equations

$$-x + 2y + z = 0$$

$$2x - y - z = 0$$

$$x + y = a$$

where a is a constant.

- (i) Investigate the arrangement of the planes:
- when $a = 0$;
 - when $a \neq 0$.
- [6]
- (ii) Chris claims that the position vectors $-\mathbf{i} + 2\mathbf{j} + \mathbf{k}$, $2\mathbf{i} - \mathbf{j} - \mathbf{k}$ and $\mathbf{i} + \mathbf{j}$ lie in a plane. Determine whether or not Chris is correct. [2]

END OF QUESTION PAPER

**Copyright Information**

OCR is committed to seeking permission to reproduce all third-party content that it uses in its assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity.

For queries or further information please contact the Copyright Team, First Floor, 9 Hills Road, Cambridge CB2 1GE.

OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.