

## **“The Knowledge” – Vital facts to know off by heart**

Discriminant and how it determines the number of roots of a quadratic

Quadratic formula

The factor theorem

Sine rule, cosine rule and area of a triangle

Equation of a circle

Graphs of sin, cos and tan (in both degrees and radians)

Special values of sin, cos and tan (in both degrees and radians)

Trigonometric identity for  $\tan \theta$ , the “Pythagorean” identity, and the two that derive from this

Laws of logarithms

Graphs of  $y = x^2$ ,  $y = x^3$ ,  $y = \frac{1}{x}$ ,  $y = \sqrt{x}$ ,  $y = a^x$ ,  $y = \log_a x$

How to determine the nature of stationary points from  $\frac{d^2y}{dx^2}$

Definitions of concave upwards and concave downwards

Derivatives of  $y = x^n$  and  $y = e^{kx}$

Graph transformations  $y = f(x) + a$ ,  $y = f(x + a)$ ,  $y = af(x)$ ,  $y = f(ax)$ ,  $y = -f(x)$ ,  $y = f(-x)$

The 5 constant acceleration formulae (SUVAT)

Special sums

$|wz|$  and  $\arg(wz)$  in terms of  $|w|$ ,  $|z|$ ,  $\arg(w)$ ,  $\arg(z)$

Modulus-argument form for a complex number with modulus  $r$  and argument  $\theta$

Complex loci for the forms  $|z - \alpha| = r$ ,  $\arg(z - \alpha) = \theta$  and  $|z - \alpha| = |z - \beta|$

Arc length and area of sector formulae given angle in radians

$n$ th terms and partial sums of arithmetic and geometric sequences (and sum to infinity)

Small angle approximations for  $y = \sin \theta$ ,  $y = \cos \theta$  and  $y = \tan \theta$

Standard matrix transformations

Inverse and determinant of  $2 \times 2$  matrices, and geometric significance of determinant

Roots of polynomials for quadratics, cubics, quartics (sums, products etc.)

Double angle formulae -  $\sin(2\theta)$ ,  $\cos(2\theta)$  (in 3 different ways) and  $\tan(2\theta)$

